

## Prediction of Monthly Streamflow at Ungauged Basin Using Flow Duration Curves

Mustafa Utku YILMAZ<sup>1\*</sup> Evren OZGUR<sup>2</sup> Kasım KOÇAK<sup>2</sup>

<sup>1</sup>Kirklareli University, Faculty of Engineering, Department of Civil Engineering, Kirklareli, Turkey

<sup>2</sup>Istanbul Technical University, Faculty of Aeronautics and Astronautics, Department of Meteorological Engineering, Istanbul, Turkey

\*Corresponding Author:

E-mail: utkuyilmaz@klu.edu.tr

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### Abstract

In order to make a reliable analysis, the requirements of the data in terms of their qualification and quantity are crucial. In this study, monthly streamflow values for target (ungauged) station were predicted by using a spatial interpolation approach based on flow duration curves. The monthly streamflow data of 5 gauge stations in Middle Euphrates basin were examined. The data contains a period of 31 years without any missing data in the dataset. In the first step of the procedure, flow duration curves (FDCs) of the 5 stations are constructed by gauged records. Each of the 5 gauge stations is assumed to be ungauged in turn. The weight values were determined by correlation coefficients. A streamflow prediction on any month at the target station was made by identifying the percentage point position on the flow duration curve of the streamflows for the same month at the source stations and reading off the streamflow value for the equivalent percentage point from the target station's duration curve. Then, each predicted streamflow value of target station was multiplied by the source station's weight. This study showed that promising results were obtained with this method, according to measured by the statistics of prediction performance, namely the Nash-Sutcliffe efficiency (NSE). The method used in this study can also be applied to other meteorological and hydrological variables such as pressure, temperature, evaporation, precipitation, etc.

**Keywords:** Monthly streamflow prediction, Flow duration curves (FDCs), Ungauged, Middle Euphrates basin, Turkey

### INTRODUCTION

In river type hydroelectric power plant projects, the streamflow values measured at the stations are of considerable utility in determining the installed power and selecting the right turbine. However, where there are no stations or where the records are short, there is a need for data estimation. Streamflows at an ungauged site of a stream are estimated using the data at another site on the same stream or in a neighboring stream. The simplest way of doing this is assuming that the flows are proportional to the drainage areas of sites [1]. Benson and Matalas (1967) conducted the earliest study of the estimation of monthly streamflow time series in ungauged areas [2]. Hirsch (1979) compared alternative approaches in predicting monthly streamflow time series [3]. Then, Fennessey (1994), Hughes and Smakhtin (1996) and Archfield et al. (2009, 2012) made daily streamflow estimation at ungauged basin using flow duration curves [4,5,6,7]. Chang Shu and Ouarda (2012) have made improvements in estimating daily streamflows with area ratio (AR) and flow duration curve (FDC) methods [8]. One of the recent studies on this area was made by Farmer and Vogel (2013). It is conducted at 1300 American Geological Survey Authority (USGS) station to estimate monthly streamflow series using various parameters [9]. The method used for estimating streamflow at ungauged site is associated with the use of commonly used FDC, which gives good results. In this study, it was intended to evaluate the monthly streamflow estimation by using a spatial interpolation approach based on flow duration curves.

### DATA and METHODOLOGY

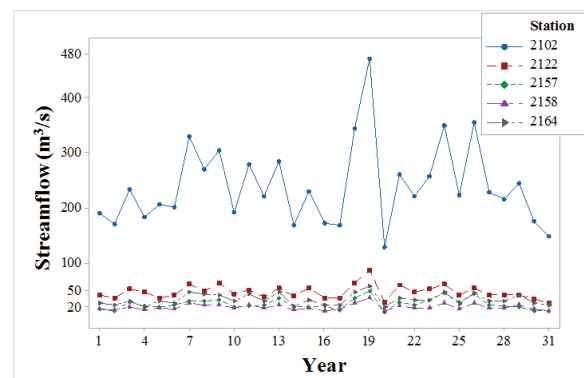
In this study, 5 streamflow gauge stations in Euphrates basin in Turkey, which is the biggest water potential selected as a case study. Each streamflow station contains a 31-year period. General information about the stations are given in Table 1. Selected stations on the map of the Middle Euphrates basin and changes of annual mean flow of these stations are shown in Figure 1 and Figure 2, respectively.

**Table 1.** General information on the gauging stations

| Station Number | Observation year | Mean streamflow (m <sup>3</sup> /s) | Drainage Area (km <sup>2</sup> ) | Basin Elevation (m) |
|----------------|------------------|-------------------------------------|----------------------------------|---------------------|
| 2102           | 1970-2000        | 239,34                              | 25515,6                          | 859                 |
| 2122           |                  | 46,56                               | 5882,4                           | 1552                |
| 2157           |                  | 24,49                               | 2098,4                           | 1250                |
| 2158           |                  | 18,88                               | 1577,6                           | 1310                |
| 2164           |                  | 32,81                               | 2232,0                           | 998                 |



**Figure 1.** Geographical locations of the gauging stations



**Figure 2.** Changes of annual mean streamflows at the stations

In this study, similar to the approach proposed by Hughes and Smakhtin (1996), the spatial interpolation method based on flow duration curve (FDC) was used. FDC is a cumulative frequency curve that shows the percentage of time that flow in a stream is likely to equal or exceed some specified value of interest. Flow rate is usually referred to as “Q”. The exceedence value as a subscript number. So,  $Q_{80}$  means the flow rate equalled or exceeded for 80% of the time.

In the first step of the procedure, flow duration curves (FDCs) of the 5 stations are constructed by gauged records. Each of the 5 gauge stations is assumed to be ungauged in turn. The selected 15 percentiles (high flow segment ( $Q_{0.1}$ ,  $Q_{0.5}$ ,  $Q_2$ ,  $Q_5$  and  $Q_{10}$ ), medium flow segment ( $Q_{40}$ ,  $Q_{45}$ ,  $Q_{50}$ ,  $Q_{55}$  and  $Q_{60}$ ), and low flow segment ( $Q_{75}$ ,  $Q_{80}$ ,  $Q_{85}$ ,  $Q_{90}$  and  $Q_{99}$ ) of FDCs) were predicted as ungauged station. The weight values (between the target station and the source station) were determined by correlation coefficients.  $r_i$  and  $r_n$  are used to find weights.  $r_i$  is the correlation coefficient,  $r_n$  is the normalized correlation coefficient, and  $n$  is the number of stations.  $r_n$  can be calculated from Equation (1).

$$r_n = \frac{r_i}{\sum_{i=1}^n r_i} \quad i, n = 1, \dots, 4 \quad (1)$$

A streamflow prediction on any month at the target station was made by identifying the percentage point position on the flow duration curve of the streamflows for the same month at the source stations and reading off the streamflow value for the equivalent percentage point from the target station’s duration curve. Then, each predicted streamflow value of target station was multiplied by the source station’s weight.

Nash-Sutcliffe efficiency (NSE) is used for prediction performance evaluation. NSE which has been proposed by Nash and Sutcliffe and is used to measure the accuracy of many hydrological forecast, is a normalized statistic [10]. The Nash-Sutcliffe efficiency, NSE, is defined as

$$NSE = 1 - \frac{\sum_{i=1}^n (X_i^{obs} - X_i^{sim})^2}{\sum_{i=1}^n (X_i^{obs} - X_i^{mean})^2} \quad (2)$$

where  $X_i^{obs}$  is the  $i$ -th observation for the monthly streamflows being evaluated,  $X_i^{sim}$  is the  $i$ -th simulated value for the monthly streamflows being evaluated,  $X_i^{mean}$  is the mean of observed data for the monthly streamflows being evaluated, and  $n$  is the total number of observations.

NSE ranges between  $-\infty$  and 1 (inclusive), with  $NSE=1$  being the optimal value. Values between 0 and 1 are generally viewed as acceptable levels of performance, whereas values  $<0$  indicates that the mean observed value is a better predictor than the simulated value, which indicates unacceptable performance.

### APPLICATION and RESULTS

The selected stations are marked in Figure 3 on the Google Earth application. Table 2 shows the Pearson correlation coefficients of the stations in matrix format. The closest and most associated / correlated stations for each station in the application region are given in Table 3. The drainage area ratio method (DAR) was used to estimate the monthly streamflow values of each of the 5 stations to compare the estimated performances of the nearest and most relevant stations as the donor station. This method is based on the equilibrium of streamflows in the unit at any month in hydrologi-

cally similar basins. Each target station is estimated with the nearest and most associated donor stations. Table 4 gives the calculated NSE values. According this results, it may be possible to obtain better results by using the most correlated station as the source station for estimation of ungauged basins.

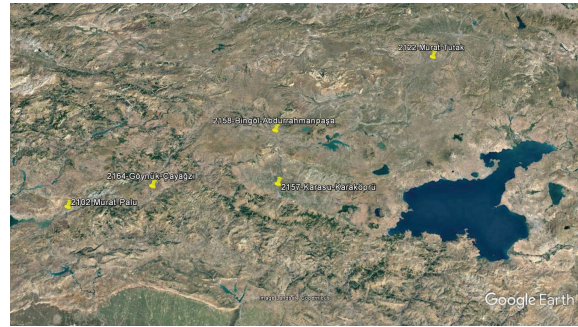


Figure 3. Streamflow gauging stations shown in Google Earth

Table 2. Correlation matrix (Pearson)

| Station Number | 2102  | 2122  | 2157  | 2158  | 2164  |
|----------------|-------|-------|-------|-------|-------|
| 2102           | 1     | 0,948 | 0,929 | 0,962 | 0,972 |
| 2122           | 0,948 | 1     | 0,807 | 0,967 | 0,889 |
| 2157           | 0,929 | 0,807 | 1     | 0,823 | 0,935 |
| 2158           | 0,962 | 0,967 | 0,823 | 1     | 0,913 |
| 2164           | 0,972 | 0,889 | 0,935 | 0,913 | 1     |

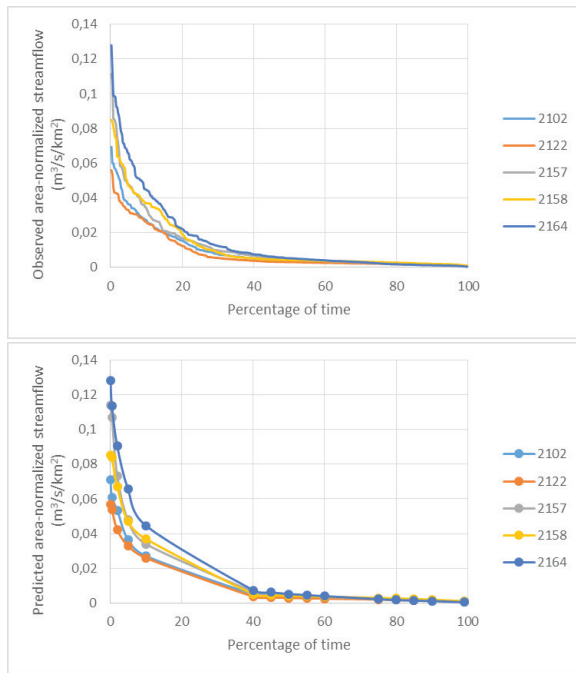
Table 3. The nearest and the most correlated stations

| Station Number | The nearest station | Euclidian distance | The most correlated station | Correlation coefficient |
|----------------|---------------------|--------------------|-----------------------------|-------------------------|
| 2102           | 2164                | 55                 | 2164                        | 0,972                   |
| 2122           | 2158                | 120                | 2158                        | 0,967                   |
| 2157           | 2158                | 36                 | 2164                        | 0,935                   |
| 2158           | 2157                | 36                 | 2122                        | 0,967                   |
| 2164           | 2102                | 55                 | 2102                        | 0,972                   |

Table 4. NSE values that are calculated from the nearest station and the most correlated station

| Target station | The nearest station used as the source station | The most correlated station used as the source station |
|----------------|--|--|
| 2102           | 0,126  | 0,126  |
| 2122           | 0,443  | 0,443  |
| 2157           | 0,652  | 0,728  |
| 2158           | 0,636  | 0,770  |
| 2164           | 0,719  | 0,719  |

Figure 4 gives the observed and estimated percentages for each station. It can be said that successful results are obtained according to the estimated and observed streamflow percentages.



**Figure 4.** Comparison of observed and predicted FDCs

The method used in this study can also be applied to other meteorological and hydrological variables such as pressure, temperature, evaporation, precipitation, etc.

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